

# Framework for Model Checking Concurrent Programs in Maude

Gorka Suárez-García

Departamento de Sistemas Informáticos y Computación  
Universidad Complutense de Madrid  
[gorka.suarez@ucm.es](mailto:gorka.suarez@ucm.es)

# Table of Contents

1. Introduction
2. The Maude System Language
3. The Echo Server Example
4. The Counterexample Transformation
5. Future Work & Conclusions

# Introduction

Algorithms are not always error-free.

How to find those errors?

- Testing = Seeking errors randomly.
- Formal verification = Machine seeking some errors.

# Model Checking

Model checking is an automatic technique for verifying whether some properties hold in a concurrent system.

$$M, s \models p$$

Where  $M$  is the model,  $s$  is the initial state, and  $p$  is the temporal logic formula to check.

# The Maude System

- Maude is a high-performance logical framework where other systems can be easily specified, executed, and analyzed.
- Maude includes a model checker for checking properties expressed in Linear Temporal Logic.

# The Maude Syntax

```
--- Functional module, used to  
--- make equational theories.
```

```
fmod SIMPLE-NATURAL is  
    sort Natural .  
    op zero : -> Natural [ctor] .  
    op s_ : Natural -> Natural [ctor] .  
    op _+_ : Natural Natural -> Natural .  
    vars N M : Natural .  
    eq zero + N = N .  
    eq s N + M = s (N + M) .  
endfm
```

```
--- System module, used to  
--- make rewriting theories.
```

```
mod SIMPLE-COUNTDOWN is  
    pr SIMPLE-NATURAL .  
    var N : Natural .  
    rl [down] : s N => N .  
endm
```

# The Maude Syntax

```
Maude> red s s s zero + s s zero .
reduce in SIMPLE-NAT : s s s zero + s s zero .
rewrites: 4 in 6729318537ms cpu (0ms real) (0 rewrites/second)
result Nat: s s s s s zero
```

```
Maude> rew s s s s s zero .
rewrite in SIMPLE-COUNTDOWN : s s s s s zero .
rewrites: 5 in 1628036047000ms cpu (0ms real) (0 rewrites/second)
result Nat: zero
```

# The Maude Syntax

```
--- Model checking property.
```

```
mod SIMPLE-PROPS is
  pr SATISFACTION .
  pr SIMPLE-COUNTDOWN .
  subsort Natural < State .
  var N : Natural .
  op cdfinished : -> Prop [ctor] .
  eq N |= cdfinished = (N == zero) .
endm
```

```
--- Model checking initial state.
```

```
mod SIMPLE-MCTEST is
  pr SIMPLE-PROPS .
  pr MODEL-CHECKER .
  pr LTL-SIMPLIFIER .
  op initial : -> Natural .
  eq initial = s s s s s zero .
endm
```

# The Maude Syntax

```
Maude> red modelCheck(initial, [](<> cdfinished)) .  
reduce in SIMPLE-MCTEST : modelCheck(initial, []<> cdfinished) .  
rewrites: 39 in 13129332125ms cpu (24ms real) (0 rewrites/second)  
result Bool: true
```

```
Maude> red modelCheck(initial, [](~ cdfinished)) .  
reduce in SIMPLE-MCTEST : modelCheck(initial, []~ cdfinished) .  
rewrites: 25 in 6264376255ms cpu (6ms real) (0 rewrites/second)  
result ModelCheckResult: counterexample({s s s s s zero,'down}  
{s s s s zero,'down} {s s s zero,'down} {s s zero,'down}  
{s zero,'down}, {zero,deadlock})
```

# The Echo Server Example in Erlang

```
-module(test).

server() ->
    register(server, self()),
    server_loop().

server_loop() ->
    receive V ->
        print(V, "\n"),
        server_loop(V)
    end.

worker() ->
    server ! "EXTERMINATE",
    server ! "ANNIHILATE",
    server ! "DESTROY".
```

# The Echo Server Syntax Tree in Selene

```
@ns(1, 'test,
  @fn(3, 'server,
    @cs(3, nil, nil,
      @op(4, @call, @lt(4, 'register), @sq(4, @lt(4, 'server)
        @op(4, @call, @lt(4, 'self), @sq(4, nil))))
        @op(5, @call, @lt(5, 'server_loop), @sq(5, nil))))
  @fn(7, 'server_loop,
    @cs(7, nil, nil,
      @rc(8, @cs(8, @lt(8, 'V), nil,
        @op(9, @call, @lt(9, 'print), @sq(9, @lt(9, 'V) @lt(9, "\n")))
        @op(10, @call, @lt(10, 'server_loop), @sq(10, nil))
      ), nil)))
  @fn(13, 'worker,
    @cs(13, nil, nil,
      @op(14, @snd, @lt(14, 'server), @lt(14, "EXTERMINATE"))
      @op(15, @snd, @lt(15, 'server), @lt(15, "ANNIHILATE"))
      @op(16, @snd, @lt(16, 'server), @lt(16, "DESTROY")))))
```

# The Selene Framework Core

- An abstract machine to run concurrent programs.
- Subsystem to handle memory and variables.
- Subsystem to handle function calls.
- Subsystem to handle message passing.
- Counterexample transformation from Maude counterexample to counterexample in JSON.

# The Erlang Interpreter Over Selene

- Semantics built using the abstract machine of Selene.
- A set of transitional rules to define the semantics using small-step semantics with a FSM to evaluate composed expressions.
- Model-checking properties defined using the abstract machine of Selene.

# The Maude Counterexample

```
reduce in TESTS :
modelCheck(testworld, [] (~ ?hasAnyFailed))
result ModelCheckResult :
counterexample(...{< 'project : Project | files : @sf("test.erl","-module(test).\n\nserver() ->\n    register(server, self()),\n    server_loop().\n\nserver_loop() ->\n        receive V ->\n            print(V, \"\\n\"),\n            server_loop(V)\n        end.\n\nworker() ->\n        server ! \"EXTERMINATE\", \n        server ! \"ANNIHILATE\", \n        server ! \"DESTROY\".",16)> < 'status : Status | nextIndex : 3, program : @ns(1,'test,@fn(3,'server,@cs(3,nil,nil,@op(4,@call,@lt(4,
'register),@sq(4,@lt(4,'server)@op(4,@call,@lt(4,'self),@sq(4,nil))))@op(5,@call,@lt(5,
'server_loop),@sq(5,nil))))@fn(7,'server_loop,@cs(7,nil,nil,@rc(8,@cs(8,@lt(8,'V),nil,@op(
9,@call,@lt(9,'print),@sq(9,@lt(9,'V)@lt(9,\"\\n\"))@op(10,@call,@lt(10,'server_loop),@sq(10,
nil))),nil)))@fn(13,'worker,@cs(13,nil,nil,@op(14,@snd,@lt(14,'server),@lt(14,
"EXTERMINATE"))@op(15,@snd,@lt(15,'server),@lt(15,"ANNIHILATE"))@op(16,@snd,@lt(16,
'server),@lt(16,"DESTROY"))))> < @id(1) : Node | cin : "", cout : "", heap : @ms(nil), info : none > < @id(1) : Process | context : @cx('test 'server,@am(@op(4,@call,@lt(4,'register),
@sq(4,@lt(4,'server)@op(4,@call,@lt(4,'self),@sq(4,nil))))@op(5,@call,@lt(5,'server_loop),
@sq(5,nil)),@InitialState,nil),@ms(nil),@vl(nothing)),messages : nil,newMsgsFlag : false,
owner : @id(1)> < @id(2) : Process | context : @cx('test 'worker,@am(@op(14,@snd,@lt(14,
'server),@lt(14,"EXTERMINATE"))@op(15,@snd,@lt(15,'server),@lt(15,"ANNIHILATE"))@op(16,
@snd,@lt(16,'server),@lt(16,"DESTROY")),@InitialState,nil),@ms(nil),@vl(nothing)),messages
: nil,newMsgsFlag : false,owner : @id(1)>, 'statement.init}..., {..., deadlock})
```

# The Counterexample Transformed

```
[{"step": "statement.init", "node": 1, "process": 1, "processes": [{"node": 1, "process": 1, "index": 4, "variables": [], "messages": [], "result": "null"}, {"node": 1, "process": 2, "index": 14, "variables": [], "messages": [], "result": "null"}]}, {"step": "statement.init", "node": 1, "process": 2, "processes": [{"node": 1, "process": 1, "index": 4, "variables": [], "messages": [], "result": "null"}, {"node": 1, "process": 2, "index": 14, "variables": [], "messages": [], "result": "null"}]}, {"step": "statement.exec", "node": 1, "process": 2, "processes": [{"node": 1, "process": 1, "index": 4, "variables": [], "messages": [], "result": "null"}, {"node": 1, "process": 2, "index": 14, "variables": [], "messages": [], "result": "<error>"}]}, {"step": "statement.error", "node": 1, "process": 2, "processes": [{"node": 1, "process": 1, "index": 4, "variables": [], "messages": [], "result": "null"}, {"node": 1, "process": 2, "index": 0, "variables": [], "messages": [], "result": "<error>"}]}, {"step": "statement.work", "node": 1, "process": 1, "processes": [{"node": 1, "process": 1, "index": 4, "variables": [], "messages": [], "result": "null"}]}, {"step": "statement.exec", "node": 1, "process": 1, "processes": [{"node": 1, "process": 1, "index": 4, "variables": [], "messages": [], "result": "null"}]}, {"step": "statement.next", "node": 1, "process": 1, "processes": [{"node": 1, "process": 1, "index": 5, "variables": [], "messages": [], "result": "null"}]}, {"step": "statement.init", "node": 1, "process": 1, "processes": [{"node": 1, "process": 1, "index": 5, "variables": [], "messages": [], "result": "null"}]}, {"step": "statement.exec", "node": 1, "process": 1, "processes": [{"node": 1, "process": 1, "index": 8, "variables": [], "messages": [], "result": "null"}]}, {"step": "statement.exec", "node": 1, "process": 1, "processes": [{"node": 1, "process": 1, "index": 8, "variables": [], "messages": [], "result": "null"}]}]
```

# The Counterexample Transformation

```
for i = 0 .. (N-1):
    c_state = counterexample.states_list[i]
    n_state = counterexample.states_list[i+1]
    process = get_changed_process(c_state, n_state)
    json_step = make_step(counterexample.rule[i], process, c_state)
    json_array.append(json_step)
```

# Counterexample Interpretation

```
1. -module(test).
2.
3. server() ->
4.     register(server, self()),
5.     server_loop().
6.
7. server_loop() ->
8.     receive V ->
9.         print(V, "\n"),
10.        server_loop(V)
11.    end.
12.
13. worker() ->
14.     server ! "EXTERMINATE",
15.     server ! "ANNIHILATE",
16.     server ! "DESTROY".
```

Colors: Process 1 & Process 2

```
{"step": "statement.init",
"node": 1,
"process": 1,
"processes": [
{"node": 1, "process": 1, "index": 4,
"variables": [], "messages": [],
"result": "null" },
{"node": 1, "process": 2, "index": 14,
"variables": [], "messages": [],
"result": "null" } ]}
```

# Counterexample Interpretation

```
1. -module(test).
2.
3. server() ->
4.     register(server, self()),
5.     server_loop().
6.
7. server_loop() ->
8.     receive V ->
9.         print(V, "\n"),
10.        server_loop(V)
11.    end.
12.
13. worker() ->
14.     server ! "EXTERMINATE",
15.     server ! "ANNIHILATE",
16.     server ! "DESTROY".
```

Colors: Process 1 & Process 2

```
{"step": "statement.init",
"node": 1,
"process": 2,
"processes":
[{"node": 1, "process": 1, "index": 4,
"variables": [], "messages": [],
"result": "null"}, {"node": 1, "process": 2, "index": 14,
"variables": [], "messages": [],
"result": "null"}]}
```

# Counterexample Interpretation

```
1. -module(test).
2.
3. server() ->
4.     register(server, self()),
5.     server_loop().
6.
7. server_loop() ->
8.     receive V ->
9.         print(V, "\n"),
10.        server_loop(V)
11.    end.
12.
13. worker() ->
14.     server ! "EXTERMINATE",
15.     server ! "ANNIHILATE",
16.     server ! "DESTROY".
```

Colors: Process 1 & Process 2

```
{"step": "statement.exec",
"node": 1,
"process": 2,
"processes":
[{"node": 1, "process": 1, "index": 4,
"variables": [], "messages": [],
"result": "null"},
 {"node": 1, "process": 2, "index": 14,
"variables": [], "messages": [],
"result": "<error>"}]}
```

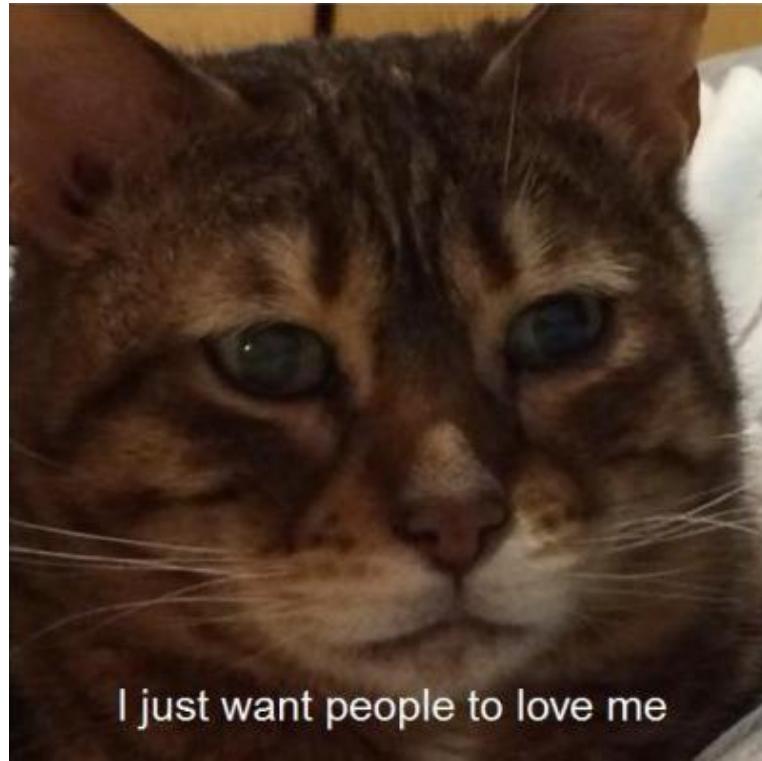
# Future Work

- Improve the core parameterization with Maude theories and views.
- Complete the semantics of the Erlang syntax.
- Add more parameterization to the counterexample transformation algorithm.
- Make a visual representation of the transformed counterexample in HTML.

# Conclusions

- The seeds of a generic abstract machine and framework to implement programming language semantics.
- A compact representation of the counterexample with meaningful information about the execution.
- Flexibility to write LTL formulae by the developer.

# Questions



I just want people to love me